

MT 1800 Calculus I
Worksheet 2.5 B – The Derivative Functions

Summary of findings up to now:

	$f(x)$
$f'(x) < 0$	<i>Decreasing</i>
$f'(x) > 0$	<i>Increasing</i>
$f''(x) < 0$	<i>Concave down</i>
$f''(x) > 0$	<i>Concave up</i>

	$f'(x)$
$f''(x) < 0$	<i>Decreasing</i>
$f''(x) > 0$	<i>Increasing</i>

What do you think? (These questions will be explored in much more detail in the future)

What happens when $f'(x)=0$?

What happens to $f(x)$ when $f'(x)$ is undefined?

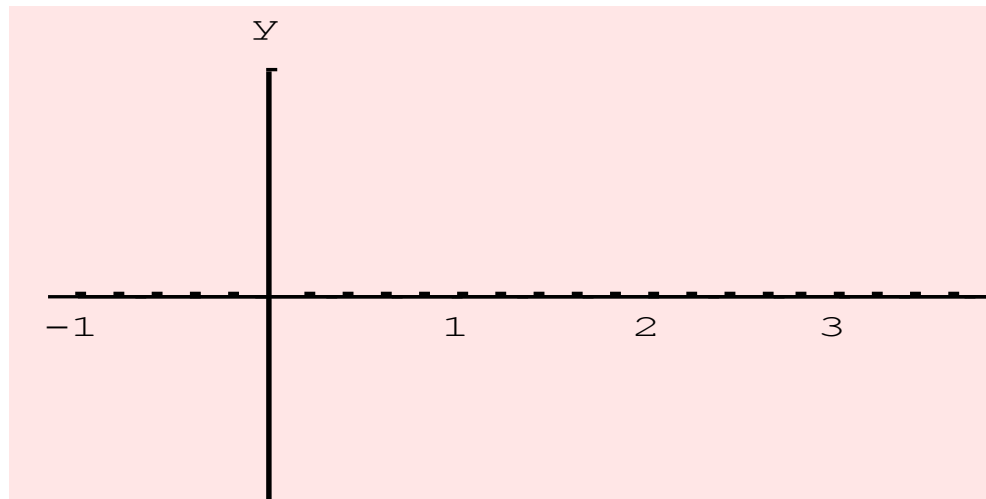
What happens to $f''(x)$ when $f'(x)$ is undefined?

What happens to $f(x)$ when $f''(x)=0$?

What happens to $f'(x)$ when $f''(x)=0$?

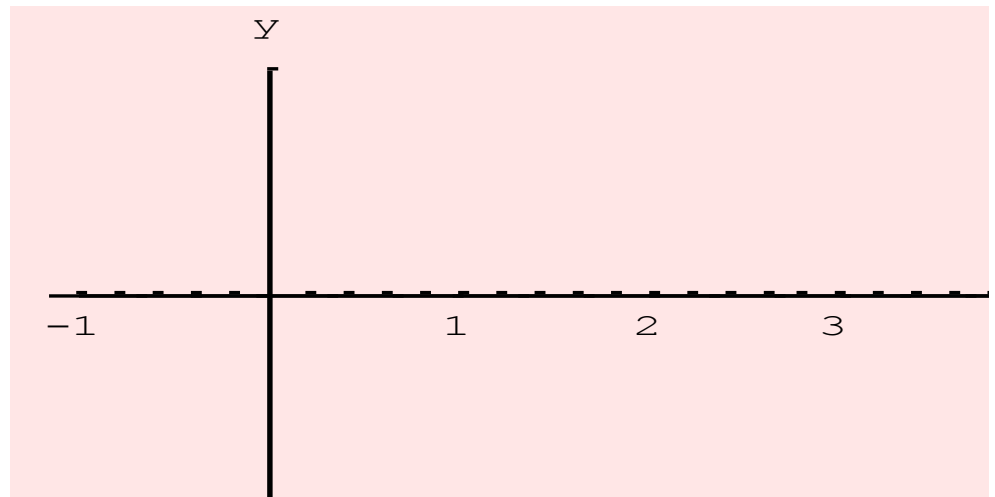
1. Sketch the graph of a continuous function that has the following characteristics:

x	(0,1)	1	(1,2)	2	(2,3)	3	(3,4)	4	5
$f(x)$	-	-	-	0	+	+	+	0	+
$f'(x)$	+	+	+	+	+	0	-	undef	+
$f''(x)$	-	0	+	0	-	-	-	undef	+

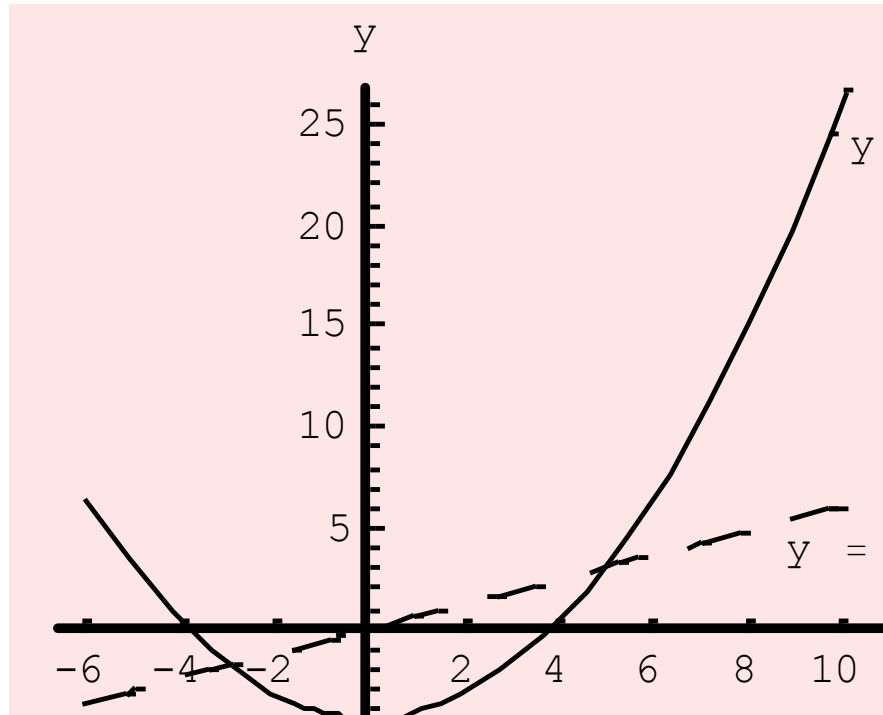


2. Sketch the graph of a continuous function that has the following characteristics:

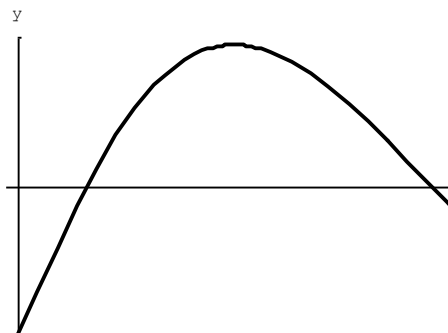
x	0	1	2	3	4	5
$f(x)$	-	-	-	-	0	+
$f'(x)$	+	0	-	0	+	+
$f''(x)$	-	-	0	+	+	+



3. On the grid below you are given the graph of both $f'(x)$ (drawn with a solid curve) and $f''(x)$ (drawn with a dotted curve). Use this information to sketch the graph of $f(x)$ on the same coordinate axes.



4. Shown below is the graph of the derivative function, $f'(x)$, for some function $f(x)$. Sketch the graph of the function $f(x)$ on the same set of axes.



5. Use the data in the table below to **estimate** the values of $f'(x)$ and $f''(x)$ for each value of x .

x	$f(x)$	$f'(x)$	$f''(x)$
1.2	25	-----	-----
1.4	28		
1.6	33		
1.8	29		
1.9	24		
2.0	27		